SAMPLE PREREQUISITE PROBLEMS: ALGEBRA II

(no calculators allowed)

Multiplication Tables (through 12)

(You will have two minutes to do the following 24 multiplication problems.)

$$2 \times 6 =$$

$$3 \times 2 = 4 \times 9 =$$

$$4 \times 9 =$$

$$5 \times 2 =$$

$$8 \times 8 =$$

$$9 \times 3 =$$

$$10 \times 7 =$$

$$2 \times 4 =$$

$$5 \times 1 =$$

$$6 \times 8 =$$

$$7 \times 9 =$$

$$8 \times 10 =$$

$$0 \times 10 =$$

$$1 \times 11 =$$

$$7 \times 3 =$$

$$11 \times 9 =$$

$$6 \times 4 =$$

$$7 \times 11 =$$

$$3 \times 7 =$$

$$4 \times 5 =$$

$$9 \times 5 =$$

$$10 \times 6 =$$

$$12 \times 10 =$$

$$9 \times 12 =$$

(Be sure that you can easily do problems like these: arithmetic with whole numbers, decimals, fractions; arithmetic with signed numbers)

$$\frac{0}{7.2} =$$

$$-\frac{(6)(-2)}{-3}=$$

$$-3 - (-2) =$$

$$1,000 \times 3.47 =$$

$$\frac{248.36}{100}$$
 =

$$\frac{1}{3} - \frac{1}{5} =$$

$$\frac{1}{3} \cdot \frac{1}{5} =$$

$$\frac{1}{3} \div \frac{1}{5} =$$

$$126 \times 24 =$$

SAMPLE PREREQUISITE PROBLEMS: ALGEBRA II

Problems 1–9 should be done WITHOUT A CALCULATOR.

1. For each expression given below, rename the expression as requested. If the requested name is not possible, so state. A few samples are done for you.

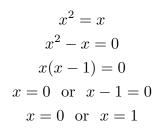
EXPRESSION	RENAME IN THIS FORM	PUT YOUR ANSWER HERE
(sample) 12 (sample) 12	a sum of even integers xy , where x and y are integers, with $x < 0$	2 + 10 or 4 + 8 etc. (-3)(-4) or (-2)(-6) etc.
(sample) 12	2^x , where $x \in \{0, 1, 2, 3, \dots\}$	not possible
$\frac{1}{\sqrt{2}}$	a fraction with no radical in the denominator	
7	a quotient of integers, where the numerator is greater than 10	
23,070,000	in scientific notation	
7	x - y, where x and y are NOT integers	
7	$\frac{1}{2} \cdot x$	
(x-2)(x+3)	as a sum (i.e., multiply out)	
$x^2 - y^2$	as a product (i.e., factor)	
$\frac{1}{2}$	$\frac{3}{x}$	
$\frac{1}{x} - \frac{2}{3+x}$	as a single fraction	
0.25	as a percent	
$x \cdot x^3 \cdot (x^2)^5$	x^k	
2 in/sec	x feet/min	
7,036	$x_1 \cdot 1000 + x_2 \cdot 100 + x_3 \cdot 10 + x_4 \cdot 1$	

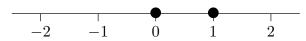
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2. Solve each equation/inequality in one variable. Write a list of equivalent sentences, ending with one that can be solved by inspection. Get EXACT answer(s), not decimal approximations. Graph each solution set on a number line. A sample is done for you.

(sample) $x^2 = x$

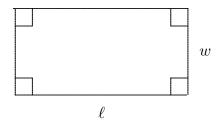
Solution:



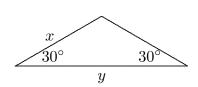


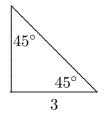
- (a) 3x(1-5x)(x-2) = 0
- (b) $\frac{1}{2}x 7 = 3x + \frac{x}{5}$
- (c) 1 2x < 3
- (d) $x^2 = x + 2$
- (e) $1 < x \text{ or } x \le -1$
- (f) 0.4(x-1) = 2x-3
- (g) $x^2 = 3$
- (h) $-1 \le x < 3$
- (i) x > -1 and $x \le 3$
- 3. Write the equation of the circle with center (1, -2) and radius 5.

- 4. Find the requested measurement(s) of each geometric figure.
 - (a) PERIMETER and AREA:

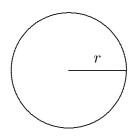


(b) PERIMETER and AREA:

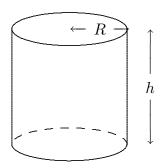




(c) CIRCUMFERENCE and AREA:



(d) VOLUME:

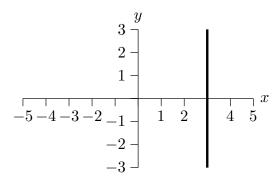


Which of the units below is a unit of length? Of area? Of volume? cubic feet $\rm cm^2$ meter

5. Graph each of the following equations/inequalities, where each sentence is viewed as a sentence in two variables. (That is, x = 3 should be viewed as x + 0y = 3.) A sample is done for you.

(sample)
$$x = 3$$

Solution:



- (a) x > 3
- (b) y = 2x 1
- (c) $y \le 2$
- (d) $(x+1)^2 + (y-3)^2 = 25$
- 6. Write an expression (using the variable x) to represent each sequence of operations.
 - (a) take a number, multiply by 2, then subtract 3
 - (b) take a number, subtract 3, then multiply by 2
 - (c) take a number, multiply it by 2, cube the result, add 1, then divide by the original number

Write the sequence of operations that is being described by each expression.

- (d) 3x 1
- (e) $2(x+1)^3 5$
- (f) $\frac{x-3}{7}-1$

- 7. Write the equation of the line, in y = mx + b form, that satisfies the given conditions.
 - (a) slope 3, passing through the point (2, -1)
 - (b) the horizontal line that crosses the y-axis at 2
 - (c) the line that is perpendicular to x 3y = 5 and passes through the point (0,3)
- 8. (Your calculator is needed for this question.)

Let
$$f(x) = \frac{1 - 3x}{x - 2}$$
.

- (a) Use your graphing calculator to graph the function f in the window -1 < x < 3 and -15 < y < 10.
- (b) Find the x-intercept of the graph.
- 9. Estimate (where necessary) each of the following numbers on your calculator. For full credit, each answer must be correct to five decimal places.

(a)
$$\frac{1+\sqrt{2}}{\sqrt[3]{5}-7}$$

(b)
$$3x^2 - 5x + 1$$
, where $x = -1.8$

(c)
$$(2.03 \times 10^{-9})(-4.1 \times 10^7)$$

SOLUTIONS

Multiplication Tables:

$$0, -4, -1$$

$$3,470, 2.4836, \frac{2}{15}$$

$$\frac{1}{15}$$
, $\frac{5}{3}$, $3,024$

1. There are many possible correct answers for this problem.

$$\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{2}}{2}$$

$$7 = 7 \cdot \frac{11}{11} = \frac{77}{11}$$

$$23,070,000 = 2.307 \times 10^7$$

$$7 = 7 + .2 - .2 = 7.2 - .2$$

$$7 = 7 \cdot \frac{1}{2} \cdot 2 = \frac{1}{2} \cdot 14$$

$$(x-2)(x+3) = x^2 + 3x - 2x - 6 = x^2 + x - 6$$

$$x^2 - y^2 = (x - y)(x + y)$$

$$\frac{1}{2} = \frac{1}{2} \cdot \frac{3}{3} = \frac{3}{6}$$

$$\frac{1}{x} - \frac{2}{3+x} = \frac{1}{x} \cdot \frac{3+x}{3+x} - \frac{2}{3+x} \cdot \frac{x}{x} = \frac{3+x-2x}{x(3+x)} = \frac{3-x}{x(3+x)}$$

$$0.25 = \frac{25}{100} = 25 \cdot \frac{1}{100} = 25\%$$

$$x \cdot x^3 \cdot (x^2)^5 = x^1 \cdot x^3 \cdot x^{10} = x^{1+3+10} = x^{14}$$

$$2\frac{\mathrm{in}}{\mathrm{sec}} = 2\frac{\mathrm{in}}{\mathrm{sec}} \cdot \frac{1 \mathrm{\ ft}}{12 \mathrm{\ in}} \cdot \frac{60 \mathrm{\ sec}}{1 \mathrm{\ min}} = 10\frac{\mathrm{ft}}{\mathrm{min}}$$

$$7,036 = 7 \cdot 1000 + 0 \cdot 100 + 3 \cdot 10 + 6 \cdot 1$$

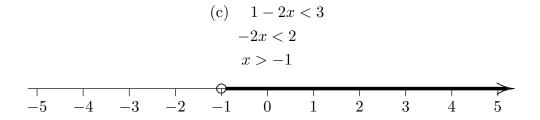
2.

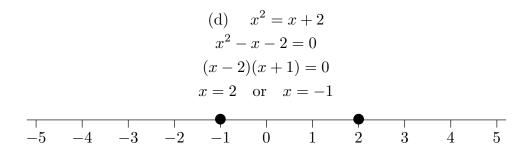
(a)
$$3x(1-5x)(x-2) = 0$$

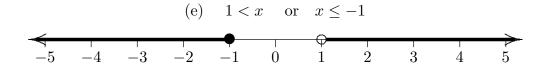
 $x = 0$ or $1-5x = 0$ or $x-2=0$
 $x = 0$ or $x = \frac{1}{5}$ or $x = 2$

(b)
$$\frac{1}{2}x - 7 = 3x + \frac{x}{5}$$

 $5x - 70 = 30x + 2x$ (clear fractions; multiply by 10)
 $-70 = 27x$
 $x = \frac{-70}{27}$
 $x = \frac{-70}{27}$



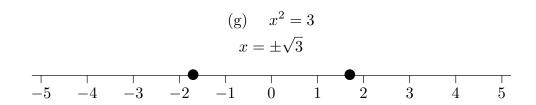


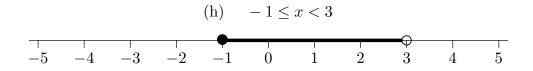


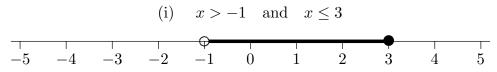
(f)
$$0.4(x-1) = 2x - 3$$

 $4(x-1) = 20x - 30$ (simplify numbers; multiply by 10)
 $4x - 4 = 20x - 30$
 $26 = 16x$
 $x = \frac{26}{16} = \frac{13}{8}$

Miss Hall's School Sample Prerequisite Problems: Algebra II—page 7 REV: 09/01







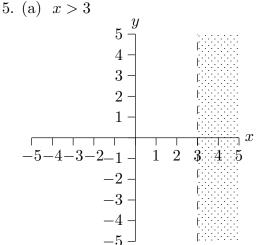
3. $(x-1)^2 + (y-(2))^2 = 5^2$ $(x-1)^2 + (y+2)^2 = 25$

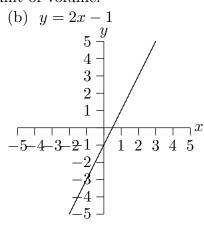
- 4. (a) PERIMETER = $2\ell + 2w$, AREA = ℓw
- (b) First triangle: PERIMETER = 2x + y, AREA = $\frac{1}{2}(y)(\frac{x}{2}) = \frac{1}{4}xy$

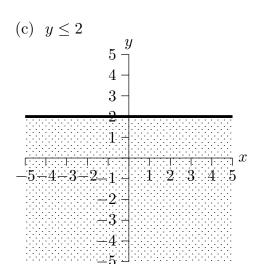
Second triangle: PERIMETER = $3+3+3\sqrt{2}=6+3\sqrt{2}$, AREA = $\frac{1}{2}(3)(3)=\frac{9}{2}$.

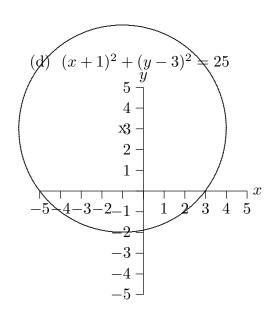
- (c) CIRCUMFERENCE = $2\pi r$, AREA = πr^2
- (d) VOLUME = (area of base)(height) = $\pi R^2 h$

Meter is a unit of length; ${\rm cm}^2$ is a unit of area; cubic feet is a unit of volume.





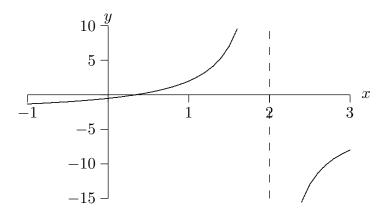




- 6. (a) 2x 3
- (b) 2(x-3)
- $(c) \quad \frac{(2x)^3 + 1}{x}$
- (d) take a number, multiply by 3, then subtract 1
- (e) take a number, add 1, cube the result, multiply by 2, then subtract 5
- (f) take a number, subtract 3, divide by 7, then subtract 1
- 7. (a) y = 3x 7
- (b) y = 2
- (c) The line x-3y=5 has slope $\frac{1}{3}$; a perpendicular line will have slope -3.

The line with slope -3 passing through (0,3) has equation y = -3x + 3.





- (b) The graph crosses the x-axis at $\frac{1}{3}$. (Set 1-3x=0. Be sure you can get this exact answer, not just $x\approx 0.333333$.)
- 9. (a) $\frac{1+\sqrt{2}}{\sqrt[3]{5}-7} \approx -0.45637$
- (b) 19.72 (this is exact)
- (d) $(2.03 \times 10^{-9})(-4.1 \times 10^7) = -0.08323$ (this is exact)